

84 Q7

Thursday, 24 September 2009  
10:06 AM

$$|\vec{V}_{A-B}| = \sqrt{18^2 + 8^2 - 2 \times 18 \times 8 \cos 80^\circ} \\ = 18.38 \text{ km/h}$$

$$\frac{\sin \theta}{8} = \frac{\sin 80^\circ}{18.38} \\ \theta = \sin^{-1} \frac{8 \sin 80^\circ}{18.38}$$

$$|\vec{AB}| = \sqrt{2^2 + 4^2 - 2 \times 2 \times 4 \times \cos 40^\circ} \\ = 2.78 \text{ km}$$

$$\frac{\sin \alpha}{4} = \frac{\sin 40^\circ}{2.78} \\ \alpha = \sin^{-1} \frac{4 \sin 40^\circ}{2.78}$$

$$= 67.65^\circ \times$$

$$\text{Bearing of B from A} = 210 - 67.65 \\ = 142.35^\circ$$

Ambiguous case. It must be the obtuse angle or we get an angle sum  $< 180^\circ$ .

$$180 - 67.65 = 112.35^\circ$$

$$112.35^\circ$$

$$142.35^\circ$$

$$97.65^\circ$$

$$105.37^\circ$$

$$B = |142.35 - 105.37|$$

$$= 36.98^\circ$$

$$7.72^\circ$$

$$BP = 2.78 \sin 36.98^\circ$$

$$= 1.67 \text{ km}$$

$$\approx 1.7 \text{ km}$$

8B Q30

$$|\vec{a} \cdot \vec{b}| = |a| |b| \cos \theta$$

$$= |a| |b| |\cos \theta|$$

$$0 \leq |\cos \theta| \leq 1$$

$$\text{so } 0 \leq |a| |b| |\cos \theta| \leq |a| |b|$$

$$\therefore 0 \leq |\vec{a} \cdot \vec{b}| \leq |a| |b|$$

